1. Lecture 1-Cycle complexes

1.1. **Bloch's cycle complex.**

1.2. **Suslin homology.**

1.3. **Suslin-Friedlander complexes.**

1.4. **Comparison theorems.**

1.5. **Products.**

2. Lecture 2-Categories of motives

2.1. **Voevodsky's geometric motives.**

2.2. **Triangulated categories of motives.**

2.3. **The Tate subcategory of $\mathcal{DM}$.**

3. Lecture 3-Cdgas, Hopf algebras and mixed Tate motives

3.1. **Dg modules over an Adams graded cdga.**

3.2. **Minimal models, co-Lie algebras and co-module categories.**

3.3. **The Bloch-Kriz category.**

3.4. **Spitzweck's representation theorem.**

4. Lecture 4-Tate motives and fundamental groups

4.1. **The fundamental exact sequence.**

4.2. **Polylog.**

4.3. **Towards a minimal model for $\mathbb{P}^1 \setminus \{0, 1, \infty\}$.**

4.4. **Tate motives over $\mathbb{Z}$-Brown's theorem.**

5. Lecture 5-π_0 and π_1 in $\mathbb{A}^1$ homotopy theory

5.1. **Motivic homotopy theory.**

5.2. **Morel's connectedness theorem.**

5.3. **Morel's theorem on π_0 of the sphere spectrum.**

5.4. **$\pi_1(\mathbb{P}^1)$ and $\pi_1(\mathbb{A}^2 - \{0\}$.**

5.5. **The motivic Steinberg relation.**

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